Scientific Programming (Wissenschaftliches Programmieren)

Exercise 4

1. Generalized Fibonacci numbers

- Create a funciion which returns "generalized" Fibonacci numbers of order *N*.
- The generalized Fibonacci numbers of order *N* should be defined as follows: The first *N* elements of the series should be 1, otherwise each element should be the sum of the previous *N* elements.
- The function should take the number of terms and the order as arguments and return an **array** containing the generalized Fibonacci numbers. The order argument should be optional with a default value of 2.
- Example calls:

```
fibonacci(10)
               2,
                       5, 8, 13, 21, 34, 55])
array([ 1, 1,
                   3,
fibonacci(10, 3)
array([ 1,
                  1,
                       З,
                           5,
                                9, 17, 31, 57, 105])
             1,
fibonacci(10, order=3)
                                9, 17, 31, 57, 105])
array([ 1,
             1,
                  1,
                       З,
                           5,
```

2. Matrix multiplication

- In order to exercise the matrix access, create a function which multiplies two matrices. For the purpose of this exercise, code the matrix multiplication algorithm by hand without using the numpy.dot() and numpy.matmul() functions or the @ operator.
- Test your function for various matrices by comparing the results against those obtained by the @ operator.
- Example:

```
m1 = np.array([[1, 2, 3], [4, 5, 6]])
m2 = np.array([[1, 2], [3, 4], [5, 6]])
matrix_product(m1, m2)
array([[ 22., 28.],
        [ 49., 64.]])
```

3. *Optimized generalized Fibonacci number algorithm

• Try to optimize the "generalized" Fibonacci number generator, so that instead of summing up *N* terms in order to create each new element, it should only use 2 arithmetic operations to generate each new element. (*N* is the order of the generalized Fibonacci numbers.)

4. *Matrix determinant

- Write a function which calculates the determinant of a square matrix. It should take the matrix as argument and return the determinant.
- Example:

```
mtx = np.array([[1.0, 2.0], [3.0, 4.0]])
determinant(mtx)
-2.0
```

• Try it with various 2x2 and 3x3 matrices and compare the result to those obtained by the numpy.linalg.det() function.